DO NOT TURN THIS PAGE UNTIL YOU ARE INSTRUCTED TO DO SO

- ❖ Write your name below on the space provided.
- ❖ This test has a total of 6 pages.
- ❖ Work the problem in the space provided. If you need more space, write on the back of the test.
- ❖ To insure maximum credit, show your work. In general, full credit will not be given for unsupported answers.
- ❖ Look only at your test. Don't give me the impression that you are cheating.
- ❖ Be sure to write neatly. If I cannot read what was written, do not expect the problem to be graded.
- ❖ If you finish early, go over the test again.

Good luck!

Number	Maximum	Score
1	2	
2	3	
3	4	
4	16	
5	8	
6	8	
7	4	
8	4	
9	4	
10	6	
11	10	
12	15	
13	16	
Total	100	

Name _____

CIRCLE FINAL ANSWERS

1) (2 points) Why do we need logarithms?

2) (3 points) Write as one logarithm $9\log_4 x + 5\log_4 y - 10\log_4 z$:

3) (4 points) Given that $\ln x = 5$, $\ln y = 10$, and $\ln z = -5$, find the exact value for $\ln \sqrt[5]{\dfrac{x^4 y}{z^5}}$:

4) (4 points each) Solve for the variable. Be sure to find the exact value.

a) $8^{2x-1} = 32^{x+4}$
                                               b) $12e^{4x+1} = 13$

c) $\log_2(x+1) - \log_2(x+2) = \log_2 8$
                     d) $\ln(3x+4) + 9 = 12$

6) (4 points) After drinking six espressos in one sitting, Mike's heartrate grew exponentially without bound. Using $f(t) = y_0 e^{kt}$ where f is the heartrate in beats per minute and t is the number of minutes after he finished his 6th espresso…

Mike was able to see a hummingbird slowly flap its wings around the 4th espresso.

a) Determine the exact value for the growth rate k if his initial heart rate was 63 beats per minute but grew to 127 beats per minute after 3 minutes.

b) Using the exact value of k from part a, determine Mike's heartrate after 10 minutes. Round to the nearest whole number:

7) (4 points each) The number of worldwide cumulative sales (in millions) of Nintendo Switch software from January 2021 to present.

Month/ Year	January 2021	April 2021	July 2021	October 2021	January 2022	April 2022
Sales (in millions)	406.67	456.49	532.34	587.12	632.4	681

Let x be the number of months since December 2020 and let y be the number of worldwide cumulative sales in millions.

a) Find an exponential regression model of the form $y = ab^x$ using your calculator. Round values to 3 decimal places.

b) Using this model, predict the month and year when there will be 800 million worldwide cumulative sales:

8) (4 points) Frank invests in the Darko Bank that offers a 1.25% simple interest rate. He invests $550 at this rate for 16 years. How much is in the account after that time?

9) (4 points) How much should be invested now so that in 15 years there will be $7,800 in an account that offers a 2.35% annual interest rate compounded quarterly?

10) (4 points) Which is a better way to invest? Option A: 6.3% compounded semi-annually or Option B: 6.25% compounded monthly? **Write answer as a percent rounded to two decimal places**.

11) (2 points each) Consider the problem below. For each part, only determine the formula that is needed to answer the question **but do not find the value. Just write the name of the formula and explain why**.

For the first 10 years of Holly's life, her parents were able to deposit $275 a month into an account that offered a 8.25% annual interest rate compounded monthly. After that time, the parents could no longer contribute to the account and just allowed the balance to sit there for the next 8 years at the same interest rate and rate of compounding.

a) Which formula would be needed to determine the amount of money in the account after the first 10 years? Explain why.

b) Which formula would be needed to determine the amount of money in the account after the 18 years? Explain why.

c) Now after those 18 years, Holly wishes to take equal withdraws from the account at the same interest rate over the next 5 years until the account has a balance of $0. Which formula would be needed and why?

12) (5 points each) Schmidt works out that he would need $5,700 a month during his retired years. He is currently 25 years old and plans to work until his is 65. He assumes that he would need to make withdraws for 30 years past his retirement and that he's in a 25% tax bracket. Assuming he finds an account that will offer him a 6.25% annual interest rate compounded monthly for the entire duration of the account…

a) How much should he have in his account at retirement?

b) How much should he deposit monthly during his working years to ensure he meets his goal?

13) Balthier is 30 years old and is working as a local sky pirate. He is able to deposit $525 a month into a Pirate Bank 401-k which offers a 7.25% annual interest rate. He does this for 30 years. After that time, he will retire. He wishes, over the next 25 years, to take out equal withdraws until the account is emptied. Assume the interest rate is the same after retirement.

a) (9 points) What are the equal withdraws he is able to take out?

b) (2 points) How much did he deposit before retirement?

c) (2 points) How much did he withdraw after retirement?

d) (2 points) How much interest did he earn overall?

14) (4 points each) Atrus borrowed $155,000 for a home on a 30-year loan that carried a 6.25% annual interest rate compounded monthly. After 12 years, he was able to refinance down to a 15-year loan that carried a 2.85% annual interest rate compounded monthly.

a) Determine the monthly payment for the beginning 30-year loan:

b) How much was left on the balance after paying for 12 years?

c) Determine the monthly payment for the new 15-year loan:

d) How much money did Atrus save by refinancing his mortgage?

CHAPTER 5 FORMULAS

Simple Interest: $I = Prt$ Amount of Simple Interest: $A = P + Prt = P(1 + rt)$

Compound Interest: $A = P\left(1 + \frac{r}{n}\right)^{nt}$ Present Value: $P = A\left(1 + \frac{r}{n}\right)^{-nt}$

Annual Percentage Yield: $APY = \left(1 + \dfrac{r}{n}\right)^{n} - 1$

Future Value of an Annuity: $FV = \dfrac{PMT\left(\left(1 + \frac{r}{n}\right)^{nt} - 1\right)}{\left(\frac{r}{n}\right)}$

Sinking Fund: $PMT = \dfrac{FV\left(\frac{r}{n}\right)}{\left(\left(1 + \frac{r}{n}\right)^{nt} - 1\right)}$

Amount Owed on a Loan: $A\left(1 + \frac{r}{n}\right)^{nt} - \dfrac{PMT\left(\left(1 + \frac{r}{n}\right)^{nt} - 1\right)}{\left(\frac{r}{n}\right)}$

Present Value of an Annuity: $PV = \dfrac{PMT\left(1 - \left(1 + \frac{r}{n}\right)^{-nt}\right)}{\left(\frac{r}{n}\right)}$

Amortization: $PMT = \dfrac{PV\left(\frac{r}{n}\right)}{\left(1 - \left(1 + \frac{r}{n}\right)^{-nt}\right)}$