

DO NOT TURN THIS PAGE UNTIL YOU ARE INSTRUCTED TO DO SO

- ❖ Write your name below on the space provided.
- ❖ This test has a total of 6 pages.
- ❖ Work the problem in the space provided. If you need more space, write on the back of the test.
- ❖ To insure maximum credit, show your work. In general, full credit will not be given for unsupported answers.
- ❖ Look only at your test. Don't give me the impression that you are cheating.
- ❖ Be sure to write neatly. If I cannot read what was written, do not expect the problem to be graded. A pencil must be used on all tests. Otherwise, the test will not be graded.
- ❖ If you finish early, go over the test again.

Good luck!

Number	Maximum	Score
1	2	
2	7	
3	4	
4	4	
5	2	
6	9	
7	6	
8	7	
9	14	
10	9	
11	20	
12	6	
13	6	
14	4	
Total	100	

Name \_\_\_\_\_



1) (2 points) Solve for the variable:  $x^4 + 34x^2 + 225 = 0$ :

2) (1 point each) For the function  $f(x) = 2x^2 + 6x + 9$ , determine...

a) If it opens up or down. How do you know?      b) The coordinates of the vertex:

c) The domain:      d) The range:      e) Interval of increase:      f) Interval of decrease:

g) Based only on your answers to parts *a* and *b*, will it have *x*-intercepts? Why or why not?

3) (4 points) A farmer has 500 feet of fence and wishes to enclose 4 adjacent rectangular pens that are all next to a river. The side against the river will not receive any fencing. Determine the dimensions of the enclosure to maximize its area. Let *x* represent the width of that enclosure. Also, what is the maximum area?

4) (2 points each) Solve for the variable. Write part *b* in interval notation:

a)  $x + \frac{12}{x-3} = 1 + \frac{4x}{x-3}$

b)  $6|2x+1| - 7 \leq 10$

5) (2 points) Fill in the chart with a sketch of the location of the arrowheads:

	Even Degree	Odd Degree
Positive Leading Coefficient		
Negative Leading Coefficient		

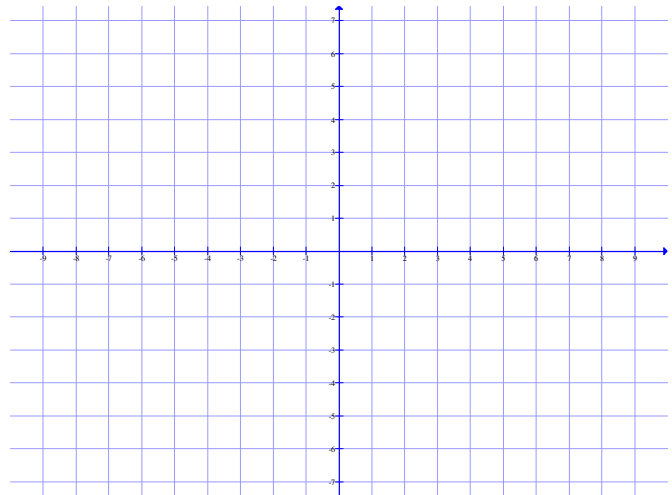
6) (3 points each) For the function  $f(x) = (x+3)^2(2x+1)^2(x-2) \dots$

a) What is the leading term and which quadrants will the arrowheads end up in? Explain why.

c) Sketch the graph based on parts a and b:

b) Fill in the chart:

Zero	Multiplicity	Touch/Cross



7) (2 points each) Form a polynomial function of degree four that meets the following requirements. **Be sure to leave your answer in factored form:**

a) Has zeros at 5,  $-8$ , 6, and 12:

b) Has the same zeros and multiplicity as in part a but is a different function:

c) Has zeros including  $2-7i$  and  $12+\sqrt{3}$ :

8) (3 points *a*; 2 points others) Consider the functions  $f(x) = 2x^3 + x^2 - 7x - 26$  and  $g(x) = x^2 + 3x + 4$ .

a) Divide  $f(x)$  by  $g(x)$  using long division:

b) Based on your work in part *a*, was  $g(x)$  a factor of  $f(x)$ ? Why or why not?

c) What is the equation of the oblique asymptote of the rational function  $y = \frac{2x^3 + x^2 - 7x - 26}{x^2 + 3x + 4}$ ?

9) (7 points each) Factor the polynomial completely by first listing the possible rational roots and then using synthetic division and your calculator.

a)  $f(x) = 3x^3 + 16x^2 + 15x - 18$

b)  $g(x) = x^5 - 11x^4 + 49x^3 - 111x^2 + 128x - 60$

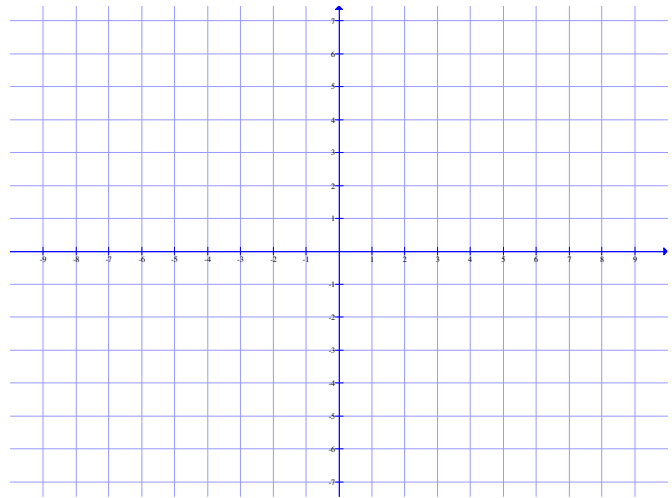
10) (3 points each) Using your factorized result from 9a, complete the following for the function  $f(x) = 3x^3 + 16x^2 + 15x - 18$ :

a) What is the leading term and which quadrants will the arrowheads end up in? Explain why.

c) Sketch the graph based on parts *a* and *b*:

b) Fill in the chart:

Zero	Multiplicity	Touch/Cross



11) (5 points each) For the function  $f(x) = \frac{2x+2}{x^2-1}$ , find...

a) The domain:

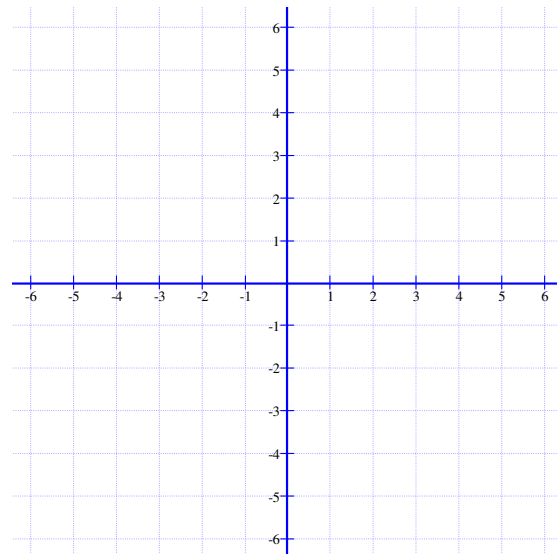
b) The intercepts (if any):

c) Any vertical asymptotes and holes:

d) Any horizontal or oblique asymptotes:

e) Sketch a graph using the above information.

**HINT:** Consider transformations based on the simplified version of the function!



12) (2 points each blank) Fill in the blank:

a) If  $c$  is a zero of a function  $f$ , then  $f(c) =$  \_\_\_\_\_, and \_\_\_\_\_ is a factor.

b) Numbers not in the domain of a rational function lead to \_\_\_\_\_.

13) (3 points each) Short answer. Clearly explain how to find the following algebraically:

a) Vertical Asymptotes and Holes:

b) Horizontal and Oblique Asymptotes:

14) (2 points each) Solve for the variable. Write answer in interval notation:

a)  $x^3 - x^2 - 6x \leq 0$

b)  $\frac{x-3}{(x-4)(x+2)} \geq 0$

Extra Credit (2 points) :

Find the equation of a rational function **in factored form** that has the following properties:

a) Hole at  $x = 7$

b) Vertical Asymptotes at  $x = -3$  and  $x = -8$

c)  $x$ -intercepts at  $x = \frac{8}{3}$  and  $x = 2$

d) Horizontal asymptote at  $y = 3$